# Means-End Relations and Artifactual Functions A Sketch

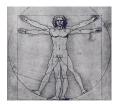
#### Jesse Hughes

Technical University of Eindhoven

June 4, 2005

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## Introduction to Norms in Knowledge



#### Epistemology:

• Knowledge of descriptive claims

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## Introduction to Norms in Knowledge



- Knowledge of descriptive claims
- Knowledge of normative claims

# Introduction to Norms in Knowledge



- Knowledge of descriptive claims
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  - Non-moral

# Introduction to Norms in Knowledge



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    - Prescriptive ought to do

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#### Applied to technical artifacts:

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Applied to technical artifacts:

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    - Prescriptive ought to do Artifacts: HOWTOs
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## Introduction to Norms in Knowledge



Applied to technical artifacts:

- Knowledge of normative claims
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    - Prescriptive ought to do Artifacts: HOWTOs
    - Functional things ought to do Artifacts: artifactual functions

## Some examples of functional ascriptions



• "The function of the heart is to pump blood."

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- "The function of the heart is to pump blood."
- "That switch mutes the television."



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We ascribe functions to biological stuff,



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We ascribe functions to biological stuff, artifacts, algorithms, personal roles...

#### How functions relate to means and ends



"That switch mutes the television."

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#### How functions relate to means and ends



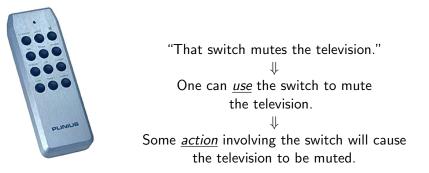
"That switch mutes the television." ↓ One can <u>use</u> the switch to mute the television.

## How functions relate to means and ends



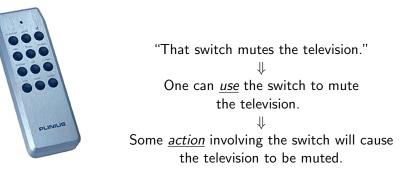
"That switch mutes the television."
↓
One can <u>use</u> the switch to mute the television.
↓
Some <u>action</u> involving the switch will cause the television to be muted.

## How functions relate to means and ends



• Functions imply means-end relations.

## How functions relate to means and ends



- Functions imply means-end relations.
- Step one: Provide a semantics for means-end relations.

# Outline

#### Means-end relations

- Propositional Dynamic Logic
- Means-end relations in PDL

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#### 2 Artifactual functions

- Functional ascriptions and fulfillment
- Normal contexts

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Basic types:a set act of <u>actions</u>,

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Propositional Dynamic Logic is a logic of actions.



Basic types:

- a set **act** of <u>actions</u>,
  - Closed under:
    - sequential composition  $\alpha; \beta$
    - <u>non-deterministic choice</u>  $\alpha \cup \beta$ .

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  - Closed under:
    - boolean connectives,
    - dynamic operators  $[\alpha]\varphi$ ,  $\langle \alpha \rangle \varphi$ .

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#### Intuitions:

•  $[\alpha]\varphi$ : after doing  $\alpha$ ,  $\varphi$  <u>will</u> hold.

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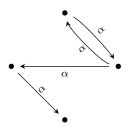


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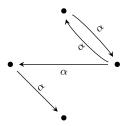
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- $[\alpha]\varphi$ : after doing  $\alpha$ ,  $\varphi$  <u>will</u> hold.
- $\langle \alpha \rangle \varphi$ : after doing  $\alpha$ ,  $\varphi$  <u>might</u> hold.



Possible world semantics with transition systems for each action  $\alpha$ .

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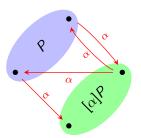


Possible world semantics with transition systems for each action  $\alpha$ .

 $w \xrightarrow{\alpha} w'$  means:

one can reach w' by doing  $\alpha$  in w.

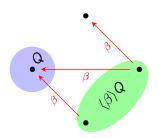
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 $\mathbf{w} \models [\alpha] \varphi \quad \underline{iff} \quad \forall \mathbf{w} \stackrel{\alpha}{\longrightarrow} \mathbf{w}' \quad \mathbf{w}' \models \varphi.$ 

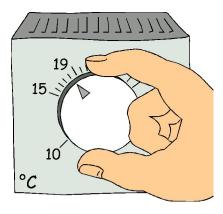


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### A thermostat example

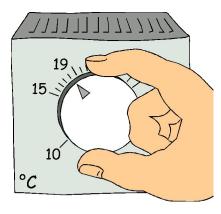


Thermostat connected to heater.

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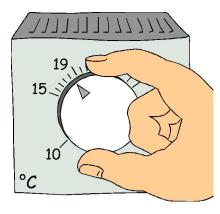
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Thermostat connected to heater. Three settings: *I*, *m*, *h* 

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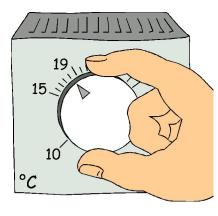
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• Setting:

$$S = h$$

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### A thermostat example



Thermostat connected to heater. Three settings: *I*, *m*, *h* 

#### Propositions:

• Setting:

• 
$$S = h$$

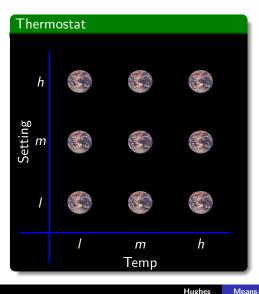
• Temperature:

• 
$$T \ge l$$

• 
$$T \ge m$$
  
•  $T \ge h$ 

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# A thermostat example

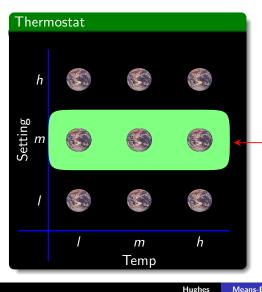


Thermostat connected to heater. Three settings: *I*, *m*, *h* Propositions: • Setting: • *S* = *I* • S = m• *S* = *h*  Temperature: • T > I• *T* > *m* •  $T \ge h$ 

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Means-End Relations and Artifactual Functions

# A thermostat example

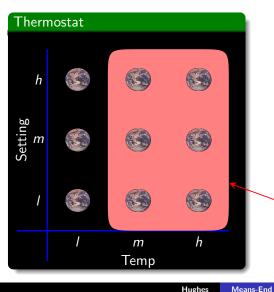


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Means-End Relations and Artifactual Functions

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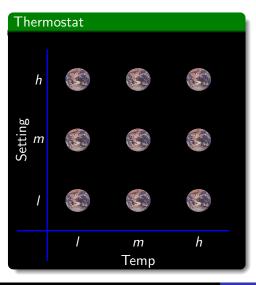


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Means-End Relations and Artifactual Functions

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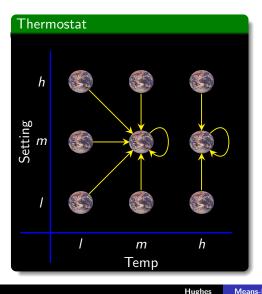


Thermostat connected to heater. Three settings: *I*, *m*, *h* <u>Actions:</u> • Change setting: • set(*I*) • set(*m*) • set(*h*)

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# A thermostat example



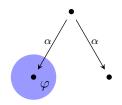
Thermostat connected to heater. Three settings: *I*, *m*, *h* <u>Actions:</u>

- Change setting:
  - **set**(/)
  - **set**(*m*)
  - **set**(*h*)
- **set**(*m*) changes:
  - setting to *m*,
  - temp  $\geq m$ .

A means is an action  $\alpha$  that can realize one's end  $\varphi.$ 

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Two interpretations:

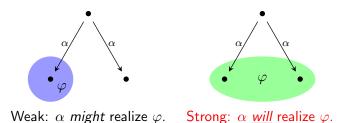


Weak:  $\alpha$  might realize  $\varphi$ .

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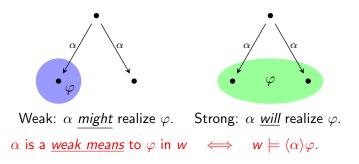
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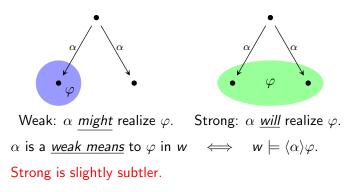
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In w,  $\alpha$  is a strongly sufficient means to  $\varphi$ 

Doing  $\alpha$  in w will yield  $\varphi$ 

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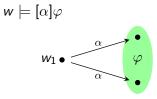
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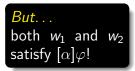
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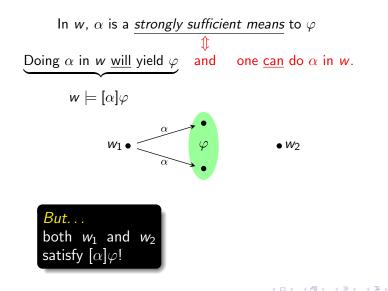


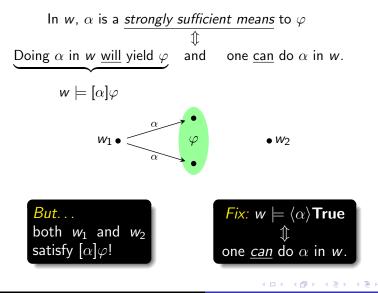


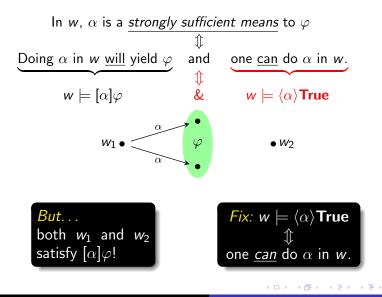
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Means-end relations Propositional Dynamic Logic Means-end relations in PDL

# Additional topics on means-end relations (All the thrilling details we won't discuss)

• Necessary means to an end.

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Means-end relations Propositional Dynamic Logic Means-end relations in PDL

Additional topics on means-end relations (All the thrilling details we won't discuss)

- Necessary means to an end.
- Conditional means-end relations.

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- Necessary means to an end.
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- Efficacy via fuzzy logic.

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#### Means-end relations

- Propositional Dynamic Logic
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#### 2 Artifactual functions

- Functional ascriptions and fulfillment
- Normal contexts

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Functional ascriptions and fulfillment Normal contexts

### Where do functions come from?

#### Historic account:

The function of o is f  $\uparrow$ the fact that o does fexplains the existence of o.

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Functional ascriptions and fulfillment Normal contexts

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Functional ascriptions and fulfillment Normal contexts

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Includes a *social* aspect.

Tough question. Let's avoid it.

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#### Functional ascriptions and fulfillment Normal contexts

# The structure of functional ascriptions

- A functional ascription f includes the following components.
  - an artifact type T,

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Context types

# The structure of functional ascriptions

- A functional ascription f includes the following components.
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    Takes parameters from

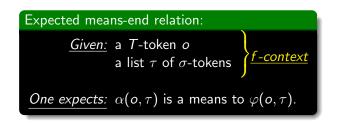
Expected means-end relation:

<u>*Given:*</u> a *T*-token oa list  $\tau$  of  $\sigma$ -tokens

One expects:  $\alpha(o, \tau)$  is a means to  $\varphi(o, \tau)$ .

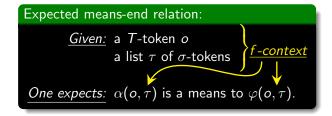
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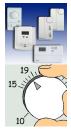


Thermostats are used to regulate temperature. Type: Thermo



Thermostats are used to regulate temperature.

Type: T hermo Parameter:  $\{l, m, h\}$ 

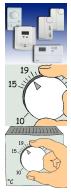


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Thermostats are used to regulate temperature.

Type: $\mathcal{T}$  hermoParameter: $\{l, m, h\}$ Action: $set_?(?)$ 

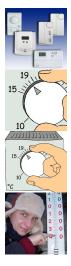


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Thermostats are used to regulate temperature.

Type: $\mathcal{T}$  hermoParameter: $\{l, m, h\}$ Action: $\mathbf{set}_{?}(?)$ End: $\mathcal{T} \geq ?$ 



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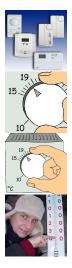
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An *f-context* is given by

• a thermostat o,



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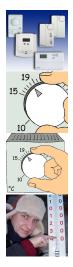
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Thermostats are used to regulate temperature.

Type: $\mathcal{T}$  hermoParameter: $\{l, m, h\}$ Action: $set_?(?)$ End: $\mathcal{T} \ge ?$ 

An *f-context* is given by

- a thermostat o,
- a setting  $x \in \{l, m, h\}$ .



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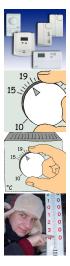
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Thermostats are used to regulate temperature.

Type:T hermoParameter: $\{I, m, h\}$ Action: $set_?(?)$ End:T > ?

An *f-context* is given by

- a thermostat o,
- a setting  $x \in \{I, m, h\}$ .
- In an *f*-context  $\langle o, x \rangle$ ,
  - our action is  $set_o(x)$ : set thermostat o to x.



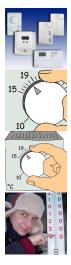
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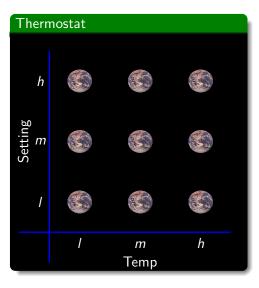
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  - our end is  $T \ge x$ .



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# Contexts and transition systems

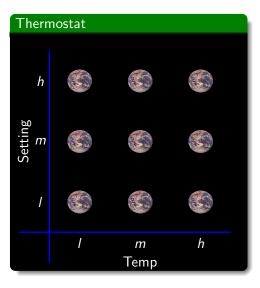


Each *f*-context  $\langle o, x \rangle$  determines a PDL model.

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Hughes Means-End Relations and Artifactual Functions

## Contexts and transition systems

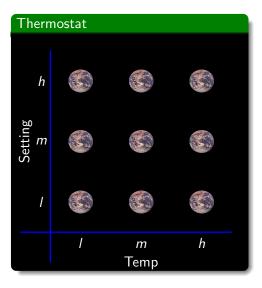


Each *f*-context  $\langle o, x \rangle$  determines a PDL model.

• o: the artifact used.

• = > •

# Contexts and transition systems

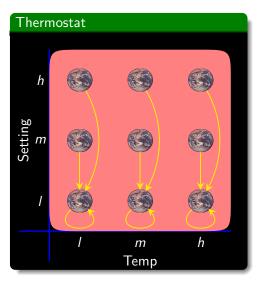


Each *f*-context  $\langle o, x \rangle$  determines a PDL model.

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- x: the setting.

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## Contexts and transition systems



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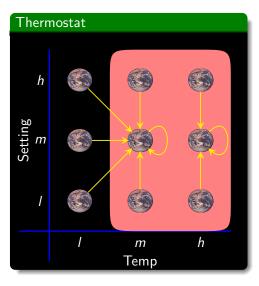
- o: the artifact used.
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Examples:

•  $\langle Working, I \rangle$ .

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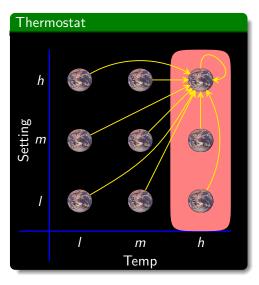
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Examples:

- $\langle Working, I \rangle$ .
- (Working, m).

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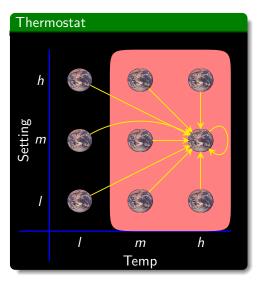
- o: the artifact used.
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Examples:

- $\langle Working, I \rangle$ .
- (Working, m).
- (Working, h).

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#### Contexts and transition systems



Each *f*-context  $\langle o, x \rangle$  determines a PDL model.

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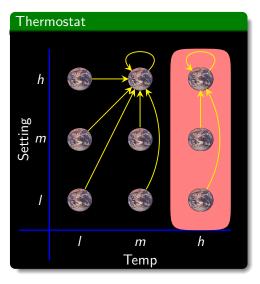
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• x: the setting.

Examples:

•  $\langle Miscal, m \rangle$ .

# Contexts and transition systems



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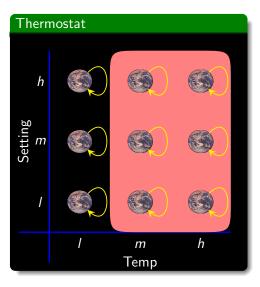
- o: the artifact used.
- x: the setting.

Examples:

•  $\langle Miscal, m \rangle$ .

•  $\langle Weak, h \rangle$ .

## Contexts and transition systems



Each *f*-context  $\langle o, x \rangle$  determines a PDL model.

- o: the artifact used.
- x: the setting.

#### Examples:

- (Miscal, m).
- $\langle Weak, h \rangle$ .
- $\langle Broke, m \rangle$ .

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## Fulfillment

#### An artifact o (weakly/strongly) fulfills f wrt $\tau$ $\uparrow$ $\alpha$ is a (weak/strong) means to $\varphi$ in $\mathcal{M}_{\langle o, \tau \rangle}$ .

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## Fulfillment

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 $\uparrow$   
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A thermostat *t* fulfills *f* wrt *x*  $\$ Setting *t* to *x* realizes  $T \ge x$ .

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#### Contexts and transition systems

Thermostat			
h			
Setting 3			
1			
	Ι	<i>m</i> Temp	h

Token	fulfills <i>f</i>
Working	I, m, h

Hughes Means-End Relations and Artifactual Functions

#### Contexts and transition systems

Thermostat			
h			
Setting 3			
I		6	
	Ι	<i>m</i> Temp	h

Token	fulfills <i>f</i>	
Working	I, m, h	
Miscal	l, m, h	

Hughes Means-End Relations and Artifactual Functions

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## Contexts and transition systems

Thermostat			
h			
Setting 3			
I			
	I	<i>m</i> Temp	h

Token	fulfills <i>f</i>	
Working	I, m, h	
Miscal	I, m, h	
Broke	1	

Hughes Means-End Relations and Artifactual Functions

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## Fulfillment

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A thermostat 
$$t$$
 universally fulfills  $f$   
 $\uparrow$   
 $t$  fulfills  $f$  wrt every  $x$ .

<u>Defined</u>: token fulfills a function f.

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<u>Defined</u>: token fulfills a function f.

When does a *subtype*  $T' \leq T$  fulfill *f*?

<u>Defined</u>: token fulfills a function f.

When does a subtype  $T' \leq T$  fulfill f?

#### Universal fulfillment:



every  $o \in T'$  fulfills f.

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<u>Defined</u>: token fulfills a function f.

When does a subtype  $T' \leq T$  fulfill f?

## Universal fulfillment:



every  $o \in T'$  fulfills f.

#### Normal fulfillment:



every "normal"  $o \in T'$  fulfills f.

Each type T comes with a set  $N_T$ of normal tokens.



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Each type T comes with a set  $N_T$  of <u>normal</u> tokens.

Are normal tokens "real" tokens?



```
Each type T comes with a set N_T of <u>normal</u> tokens.
```

Are normal tokens "real" tokens? NO!

every T-token is broken xnormal T-tokens are broken.



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```
Each type T comes with a set N_T of <u>normal</u> tokens.
```

Are normal tokens "real" tokens? NO!

every *T*-token is broken **X** normal *T*-tokens are broken.

```
Normal tokens are useful fictions.
Express how T-things are expected to behave.
```



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#### Normal tokens: the excuses

We add fictional objects to our semantics? What are you thinking?



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#### Normal tokens: the excuses

We add fictional objects to our semantics?

What are you thinking?

• Counterfactuals bad. Fictions barely worse.



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We add fictional objects to our semantics?

What are you thinking?

- Counterfactuals bad. Fictions barely worse.
- Fictional tokens approximate intuitions.



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- Formally simple, conceptually opaque.
- Gives sense of malfunction.



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We add fictional objects to our semantics?

What are you thinking?

- Counterfactuals bad. Fictions barely worse.
- Fictional tokens approximate intuitions.
- Formally simple, conceptually opaque.
- Gives sense of malfunction.
- Distinguishes subtypes.



## Normal tokens: subtypes

Subtypes do not always inherit functional ascriptions.



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# Normal tokens: subtypes

Subtypes do not always inherit functional ascriptions.

```
f is a function of T and T' \leq T

X

T' fulfills f.
```



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# Normal tokens: subtypes

Subtypes do not always inherit functional ascriptions.

f is a function of T and  $T' \leq T$  XT' fulfills f.

 $\frac{\text{Universal fulfillment:}}{T \text{ fulfills } f} \Rightarrow T' \text{ fulfills } f$ 



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# Normal tokens: subtypes

Subtypes do not always inherit functional ascriptions.

f is a function of T and  $T' \leq T$  XT' fulfills f

 $\begin{array}{rcl} \underline{\text{Universal fulfillment:}} & T \text{ fulfills } f \implies T' \text{ fulfills } f \\ \hline \underline{\text{Normal fulfillment:}} & T \text{ fulfills } f & \underline{and} & N_{T'} \subseteq N_T \implies T' \text{ fulfills } f \end{array}$ 



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# Normal tokens: subtypes

Subtypes do not always inherit functional ascriptions.

```
f is a function of T and T' \leq T

\overset{\bullet}{\underbrace{}}
T' \text{ fulfills } f.
```

 $\begin{array}{rcl} \underline{\text{Universal fulfillment:}} & T \text{ fulfills } f & \Rightarrow & T' \text{ fulfills } f \\ \underline{\text{Normal fulfillment:}} & \\ T \text{ fulfills } f & \underline{and} & N_{T'} \subseteq N_T & \Rightarrow & T' \text{ fulfills } f \end{array}$ 

Normal flare guns aren't normal guns.



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• A philosophical treatment of "normal tokens".

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- A philosophical treatment of "normal tokens".
- Add efficacy to functions.

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- A philosophical treatment of "normal tokens".
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- A philosophical treatment of "normal tokens".
- Add efficacy to functions.
- A formalization of malfunction.
- Types and function inheritance.

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- A philosophical treatment of "normal tokens".
- Add efficacy to functions.
- A formalization of malfunction.
- Types and function inheritance.
- Everything else.

-2